



<http://elec3004.com>

Information Theory

ELEC 3004: **Systems**: Signals & Controls

Dr. Surya Singh & Timothy Sherry

Lecture 24

(with material from [D. MacKay](#), B. Lathi, [K. Harris](#), [D. Corrigan](#), and more!)

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<http://robotics.itee.uq.edu.au/~elec3004/>

May 29, 2019

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Lecture Schedule:

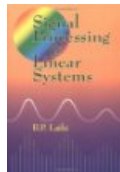
Week	Date	Lecture Title
1	27-Feb	Introduction
	1-Mar	Systems Overview
	6-Mar	Systems as Maps & Signals as Vectors
2	8-Mar	Systems: Linear Differential Systems
	13-Mar	Sampling Theory & Data Acquisition
3	15-Mar	Aliasing & Antialiasing
	20-Mar	Discrete Time Analysis & Z-Transform
	22-Mar	Second Order LTID (& Convolution Review)
4	27-Mar	Frequency Response
	29-Mar	Filter Analysis
5	3-Apr	Digital Filters (IIR) & Filter Analysis
	5-Apr	PS 1: Q & A
6	10-Apr	Digital Windows
	12-Apr	Digital Filter (FIR)
7	17-Apr	Active Filters & Estimation
	19-Apr	Holiday
	24-Apr	
	26-Apr	
8	1-May	Introduction to Feedback Control
	3-May	Servoregulation & PID Control
9	8-May	State-Space Control
	10-May	Guest Lecture: FFT
10	15-May	Advanced PID & FFT Processes
	17-May	State Space Control System Design
11	22-May	Shaping the Dynamic Response
	24-May	Stability and Examples
12	29-May	System Identification & Information Theory & Information Space
	31-May	Summary and Course Review



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Follow Along Reading:



B. P. Lathi
*Signal processing
and linear systems*
1998
[TK5102.9.L38 1998](#)



**David J. C.
MacKay**
*Information Theory,
Inference and Learning
Algorithms*
2003

[http://www.inference.
phy.cam.ac.uk/itila/](http://www.inference.phy.cam.ac.uk/itila/)

Today

→ Information Theory ←

- Lathi Ch. 2 (?)
 - § 2.7-6 Time Constant and Rate of Information Transmission
- Information Theory!

- Final Exam Review:
[http://robotics.itee.uq.
edu.au/~elec3004/tutes.h
tml#Final](http://robotics.itee.uq.edu.au/~elec3004/tutes.html#Final)

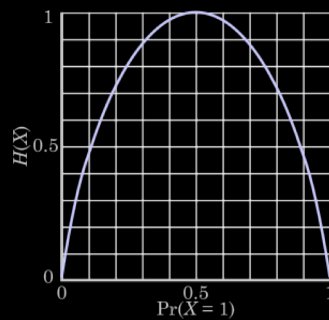
Next Time



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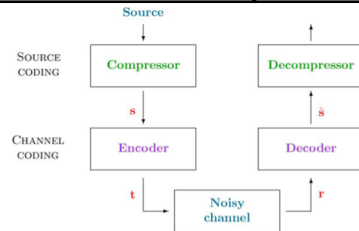
Information Theory!



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Shannon Information Theory



“The fundamental problem of communication is that of reproducing at one point, either exactly or approximately, a message selected at another point.”

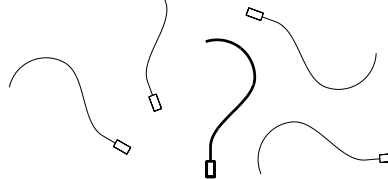
On the transmission of information over a noisy channel:

- An **information source** that produces a message
- A **transmitter** that operates on the message to create a signal which can be sent through a channel
- A **channel**, which is the medium over which the signal, carrying the information that composes the message, is sent
- A **receiver**, which transforms the signal back into the message intended for delivery
- A **destination**, which can be a person or a machine, for whom or which the message is intended



Information theory is...

- It all starts with **Probability Theory!**



1. (Wikipedia) Information theory is a branch of applied mathematics, electrical engineering, and computer science involving the quantification of information.
2. Information theory is **probability theory** where you take logs to base 2.

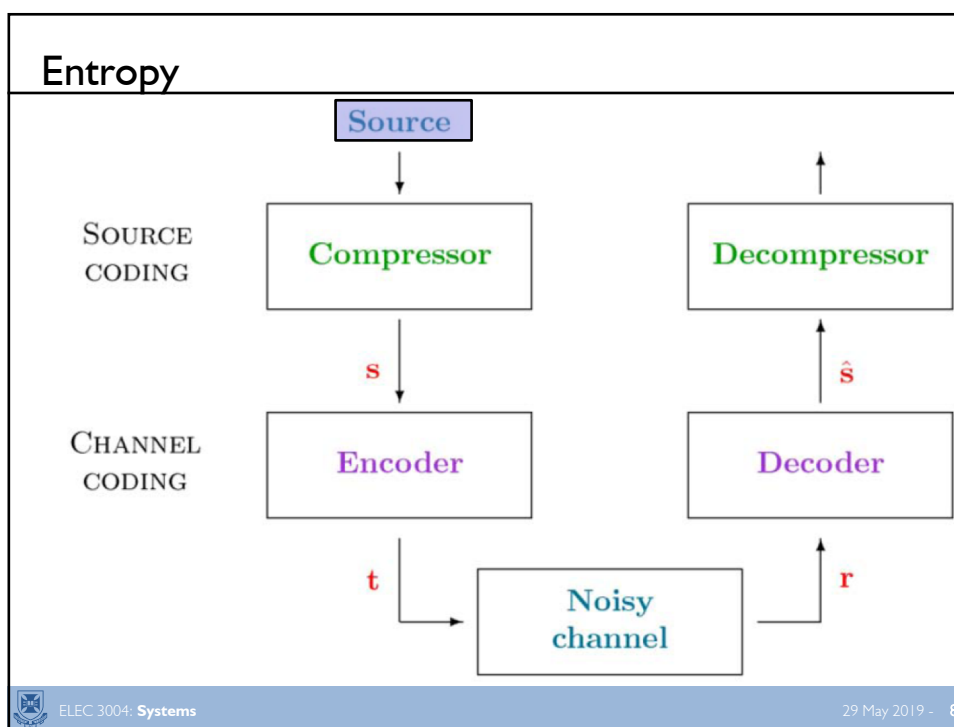


Entropy

Entropy! 😊

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Entropy – a measure of randomness

- **Entropy**

The entropy of a random variable X with a probability mass function $p(x)$ is defined by

$$H(X) = - \sum_x p(x) \log_2 p(x). \quad (1.1)$$

Example 1.1.2 Suppose that we have a horse race with eight horses taking part. Assume that the probabilities of winning for the eight horses are $(\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{64}, \frac{1}{64}, \frac{1}{64}, \frac{1}{64})$. We can calculate the entropy of the horse race as

$$\begin{aligned} H(X) &= -\frac{1}{2} \log \frac{1}{2} - \frac{1}{4} \log \frac{1}{4} - \frac{1}{8} \log \frac{1}{8} - \frac{1}{16} \log \frac{1}{16} - 4 \frac{1}{64} \log \frac{1}{64} \\ &= 2 \text{ bits.} \end{aligned} \quad (1.3)$$



Entropy

- Consider the Random Variable X , the outcome of each consecutive horse race.
- Assigning a binary number to each horse in the race would require $8 = 2^k \rightarrow k = 3 \text{ bits/symbol}$
- Shannon states that some encoding scheme on the sequence $X_1, X_2 \dots X_n$ can reduce the average number of bits $\rightarrow H(X) = 2 \text{ bits/symbol}$
- We will show you how soon



Connection to Physics

- A macrostate is a description of a system by large-scale quantities such as pressure, temperature, volume.
- A macrostate could correspond to many different microstates i , with probability p_i .
- Entropy of a macrostate is
- $S = -k_B \sum_i p_i \ln p_i$



Entropy: The bent coin

Example 2.1.1 Let

$$X = \begin{cases} 1 & \text{with probability } p, \\ 0 & \text{with probability } 1 - p. \end{cases} \quad (2.4)$$

Then

$$H(X) = -p \log p - (1 - p) \log(1 - p) \stackrel{\text{def}}{=} H(p). \quad (2.5)$$

- Consider X to be the result of a coin toss.
- This coin has been modified to land a Head (1) with probability p and Tails (0) with probability $1-p$.
- What is the entropy of X as we vary p ?

Plot a graph of $H(p)$ against p .



Entropy

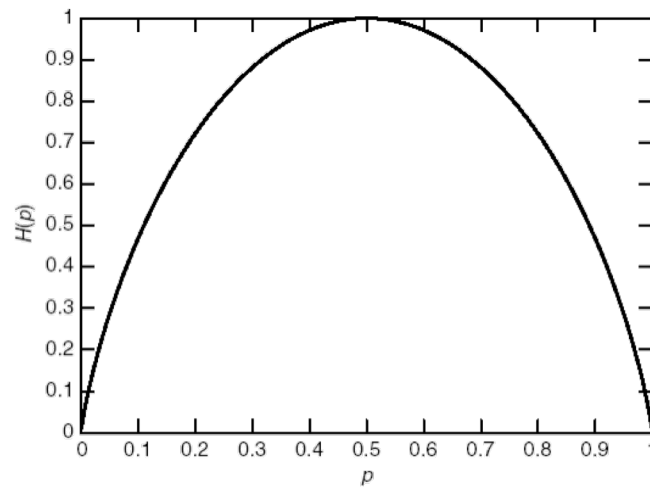


FIGURE 2.1. $H(p)$ vs. p .



Bent/Unfair Coin

- The most unpredictable coin is the fair coin.
- More generally for a variable of k states, a uniform distribution across all k states exhibits maximum entropy
- The observation of a coin with two tails is not random at all.



Example: Mystery Text

- I. Emma Woodh*use, hands*me, clever* and rich,*with a comiortab*e home an* happy di*position,*seemed to*unite som* of the b*st bless*ngs of existence;*and had *ived nea*ly twenty *ne year* in the*world w*th very*little *o distr*ss or vex*her. *he was*the yo*ngest *f the *wo dau*hters *f a most *ffect*onate* indu*gent *ather* and *ad, i* cons*quenc* of h*r sister'* mar*iage* bee* mis*ress*of h*s ho*se f*om a ver* ea*ly *erid. *er *oth*r h*d d*ed *oo *ong*ago*for*her to*have *or* t*an*an*in*is*in*t *em*mb*an*e *f *er*ca*es*es* a*d*h*r*p*a*e*h*d*b*e* *u*p*i*d*b* *n*ec*le*t*w*m*n*a* g**e**e**,**h**h** *l**n**i**l**s**r**o**a**o**e**i** a***c***n***S***e***y***s***d***s***a***r***e***n*** W****o****s****j****l****a****g****n****t****a****e****v****
- II. Emma Woodhouse, handsome, clever, and rich, with a comfortable home and happy disposition, seemed to unite some of the best blessings of existence; and had lived nearly twenty one years in the world with very little to distress or Vex her. She was the youngest of the two daughters of a most affectionate, indolent father; and had , in consequence of her sister's marriage , been mistress of his house from a very early period. Her mother had died too long ago for her to have more than an indistinct remembrance of her caresses; and her place had been supplied by an excellent woman as governess, who had fallen little short of a mother in affection. Sixteen years had Miss Taylor been in Mr Woodhouse's family , less as a eoverness than a friend , very

Entropy of English - 2.6 Bits/letter || Raw encoding $27 \times 4 = 31$ sym = 5.1 Bits/letter

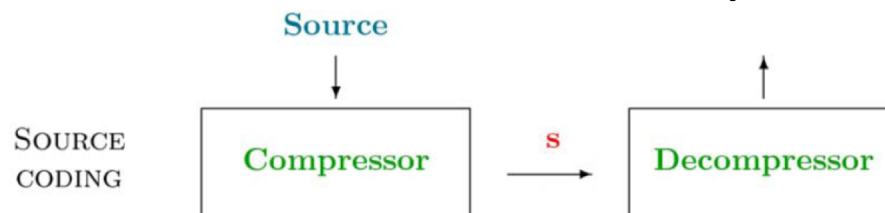
Source: MacKay VideoLectures 02, Slide 5



Source coding

Data Compression/Source coding

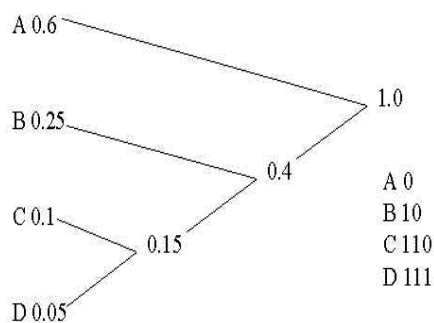
- **Removes** redundancy to reduce bit length of messages
- Save bits on common symbols/sequences
- Spend extra bits on the 'surprises', as they very rarely occur
- Lossless (Huffman, Algorithmic, LZ, DEFLATE)
- Lossy (JPEG, MP3, H.265 etc)
- Lossy techniques exploit perceptual dynamic range to expend bits where a human is sensitive, and save where they're not



Huffman Coding

- Huffman is the simplest entropy coding scheme
 - It achieves average code lengths no more than 1 bit/symbol of the entropy

- A binary tree is built by combining the two symbols with lowest probability into a dummy node
- The code length for each symbol is the number of branches between the root and respective leaf

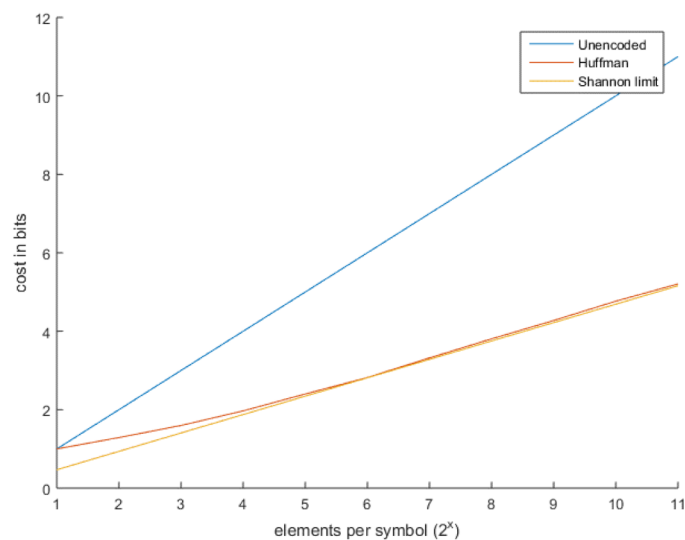


Ex: Bent/Unfair Coin

- Form symbols TT, HT, TH, HH
- $P(TT) = 0.81$; $P(HT) = P(TH) = 0.09$; $P(HH) = 0.01$
- $X_{TT} = 0 \mid p = 0.81$ $X_{TH} = 10 \mid p = 0.09$
 $X_{HT} = 110 \mid p = 0.09$ $X_{HH} = 111 \mid p = 0.01$
- Transmission cost $0.81 \cdot 1 + 0.09 \cdot 2 + 0.09 \cdot 3 + 0.01 \cdot 3 = 1.29 \frac{\text{bits}}{\text{symbol}}$
- $H(X) = 0.4690 \cdot 2 = 0.938 \frac{\text{Bits}}{\text{symbol}}$ – non-optimal code
- Huffman transmission cost $H(X) \leq C < H(X) + 1 \frac{\text{bit}}{\text{symbol}}$
- longer code words = better performance



Huffman performance -> Longer codewords



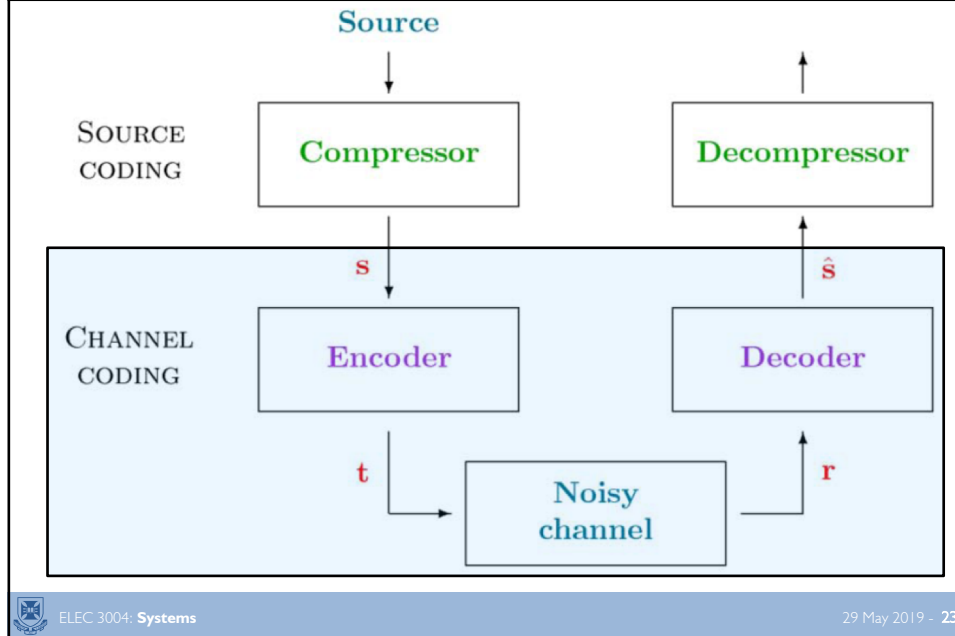
Lossless compression and entropy

- The lower the entropy of the source, the more we can gain via compression.
- The fair coin exhibits no exploitable means of **compressing** a sequence of observations from their direct description, without losing some information in the process
- All forms of compression exploit structure to reduce the average number of bits to describe a sequence.



Channel Coding

Channel and Source Coding



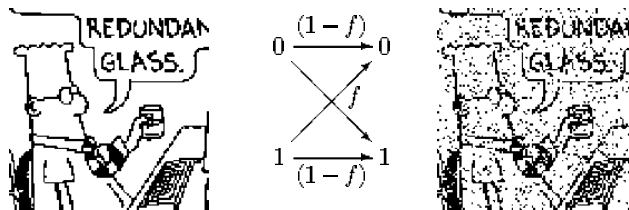
Channel coding

- All physical transmission is susceptible to noise.
- Noise results in errors when a transmission is converted back to the source space
- Channel coding **introduces** redundancy to reduce the probability an error is made in conversion back to the source.

Noisy channels: Binary Symmetric Channel

$$\begin{array}{ccc}
 \begin{array}{c} x \\ 0 \rightarrow 0 \\ 1 \rightarrow 1 \end{array} & \begin{array}{c} y \\ 0 \\ 1 \end{array} & \begin{array}{l} P(y=0|x=0) = 1-f; \quad P(y=0|x=1) = f; \\ P(y=1|x=0) = f; \quad P(y=1|x=1) = 1-f. \end{array}
 \end{array}$$

- A 1 bit digital channel where each bit experiences a probability, f , of being misinterpreted (flipped)
- Ex: A File of $N=10,000$ bits is transmitted with $f=0.1$



How many bits are flipped?

Assume a Binomial distribution

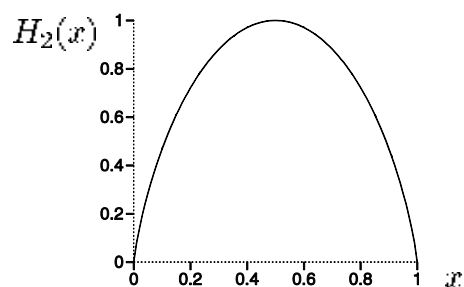
- Mean: $\mu = Np$
- Variance: $\sigma^2 = Npq$

Then:

$$\begin{aligned}
 \mu &= (0.1)10,000 \\
 \sigma^2 &= (0.1)(0.9)10,000 = 900
 \end{aligned}$$

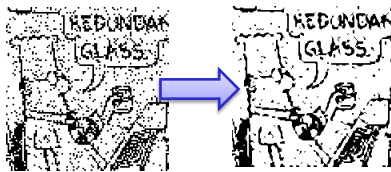
Thus:

$$1000 \pm 30$$



How to beat this?

Filter like mad!



- But this will also affect “non-noisy” signal portions

Matlab: `medfilt2(noisy_im)`

Redundant Transmission!

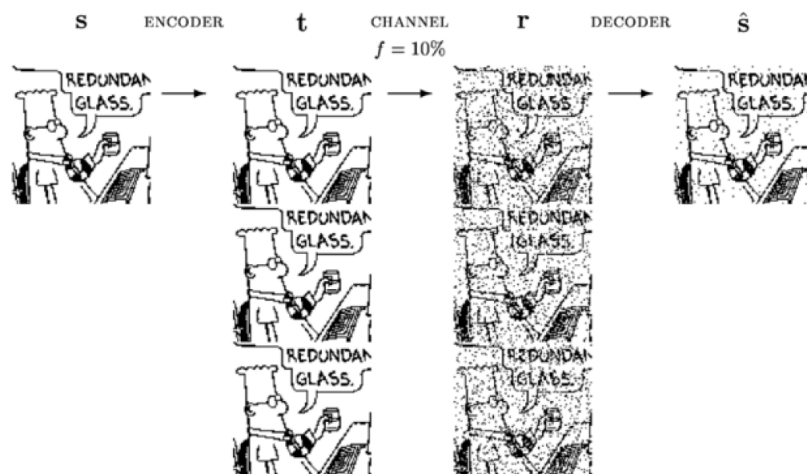


- Repetition Code ‘R3’

$$r = t \bmod 2^n$$
- Does there exist some scheme where $P(\text{error}) \rightarrow 0$
- Can we quantify the required redundancy?



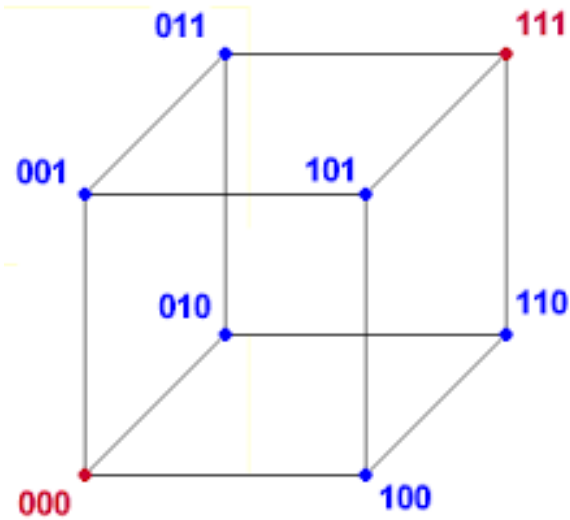
Repetition Code ‘R3’



Source: MacKay VideoLectures 01, Slide 30



Hamming distance of R3

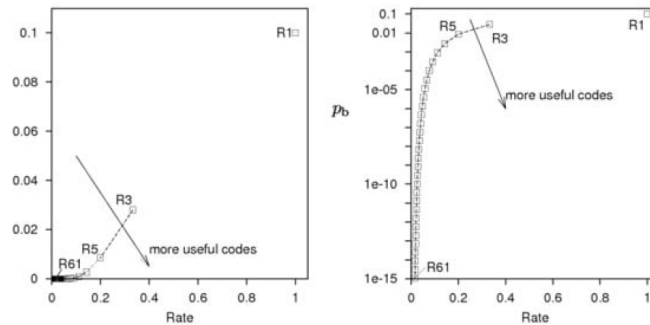


P_{error} of the R₃ code

- $P(r_{000}, s_1) = P(r_{111}, s_0) = 0.1^3 = 0.001$
- $P(r_{100}, s_1) = P(r_{010}, s_1) \dots = 0.1^2 = 0.01$
- $P_{err} = (0.001 + 0.01 \cdot 3) \cdot p(s_1) + (0.001 + 0.01 \cdot 3) \cdot p(s_0)$
- $P_{err} = 0.031$
- The number of errors $\mu = 310 \pm 17.3$
- Approximately 3x reduction in errors, but 3x as many bits required to send the message



Performance of Repetition Codes



- Want to maximise rate, minimise Error
- Software (e.g. Checksums) can identify errors and correct to higher stringency
- Can we do better?

Source: MacKay VideoLectures 01, Slide 45

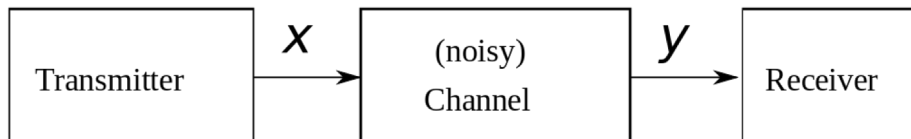


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The Noisy-channel coding theorem

- The channel capacity for the general channel:



- Is the **mutual information** between X and Y:

$$\text{Capacity} = I(X; Y)$$
- We will show Capacity of the BSC is:

$$\text{Capacity}_{BSC} = I(X_{BSC}; Y_{BSC}) = 1 - H(P_{BSC})$$
- Where H is the **Shannon entropy** of the bent coin with P_{BSC}



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Conditional Entropy

- Suppose Alice wants to tell Bob the value of X
 - And they both know the value of a second variable Y .
- Now the optimal code depends on the conditional distribution $p(X|Y)$
- Code length for $X = i$ has length $-\log_2 p(X = i|Y)$
- Conditional entropy measures average code length when they know Y

$$H(X|Y) = - \sum_{X,Y} p(X,Y) \log_2 p(X|Y)$$



Mutual information

- How many bits do Alice and Bob save when they both know Y ?

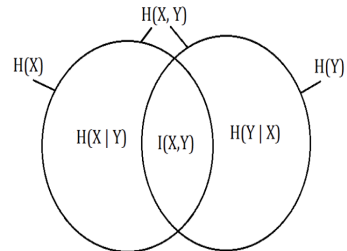
$$\begin{aligned} I(X; Y) &= H(X) - H(X|Y) \\ &= \sum_{X,Y} p(X,Y) (-\log_2 p(X) + \log_2 p(X|Y)) \\ &= \sum_{X,Y} p(X,Y) \log_2 \left(\frac{p(X,Y)}{p(X)p(Y)} \right) \end{aligned}$$

- Symmetrical in X and Y !
- Amount saved in transmitting X if you know Y equals amount saved transmitting Y if you know X .



Properties of Mutual Information

$$\begin{aligned}
 I(X; Y) &= H(X) - H(X|Y) \\
 &= H(Y) - H(Y|X) \\
 &= H(X) + H(Y) - H(X, Y)
 \end{aligned}$$

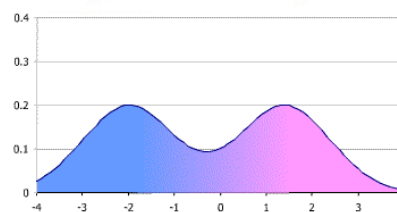
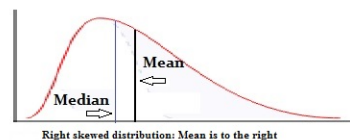
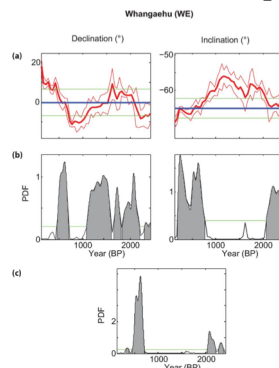


- If $X = Y$, $I(X; Y) = H(X) = H(Y)$
- If X and Y are independent, $I(X; Y) = 0$
 $H(X, Y) = H(X) + H(Y|X) = H(Y) + H(X|Y)$ $H(X|Y) \leq H(X)$
- In straightforward terms, information is never negative, we are always at least as certain about $X|Y$ vs X



Conditional Entropy & Mutual Information

- Note that the distributions $p(X)$, $p(Y)$ and $p(X|Y)$ may be complex.
- computing $p(X|Y)$ may be intractable
- Mutual Information and Conditional entropy hold for all distributions, but quantifying them may be intractable



Mutual information of the $BSC_{p=0.1}$

$$P(X_0, Y_0) = P(X_1, Y_1) = 0.5 * 0.9 = 0.45$$

$$P(X_0, Y_1) = P(X_1, Y_0) = 0.5 * 0.1 = 0.05$$

$$P(X_0) = P(X_1) = P(Y_0) = P(Y_1) = 0.5$$

$$I(X; Y) = \sum_{x, y} p(x, y) \log_2 \left(\frac{p(x, y)}{p(x)p(y)} \right)$$

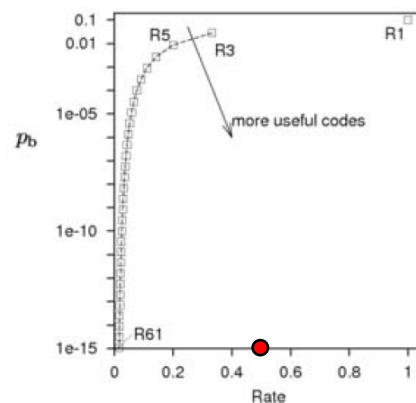
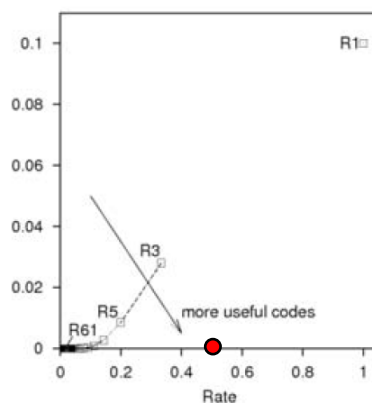
$$I(Y; Y) = 2 \cdot 0.45 \log_2 \left(\frac{0.45}{0.5^2} \right) + 2 \cdot 0.05 \log_2 \left(\frac{0.05}{0.5^2} \right)$$

$$I(Y; Y) = 0.7632 - 0.2322 = 0.531$$

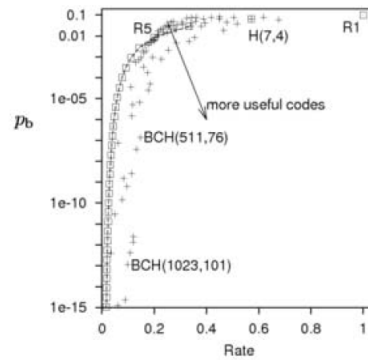
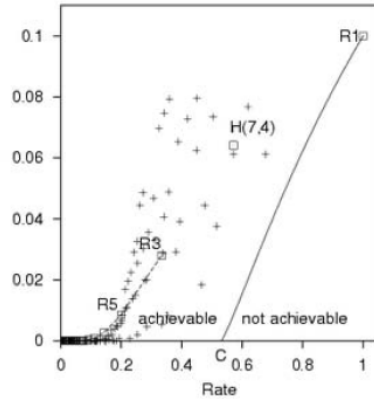


Ultimate error free performance

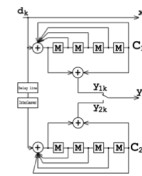
- $H(0.1) = 0.4690$
- Capacity = 0.531 Bits per Symbol
- Theoretically can obtain a $p_b = 0$ at that rate
- Does not tell us how to obtain that rate



What's Practically Achievable?



- Iterative forward error correction (FEC) codes
- Shannon told us the limit, reaching it is not so easy



Source: MacKay VideoLectures 01, Slide 54



Break ☺

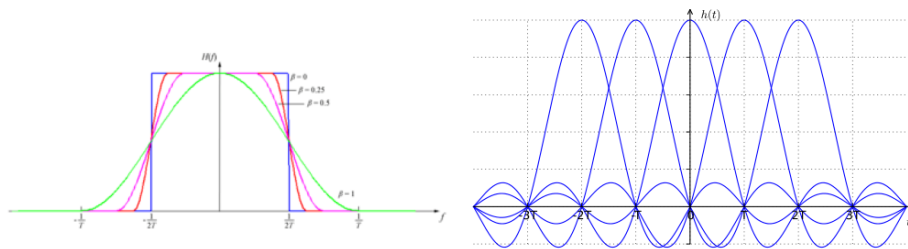
Communications

Physical layer – Modulation Schemes

- The final piece to transmitting over real communication channels
- Analog modulation (AM (SSB) ,FM , PM, QAM)
- Digital modulation(ASK,PSK,FSK,QAM)
- Both encode the signal on the amplitude (A) or phase (F,P,Q) of a carrier sine frequency
- Will only cover digital Quadrature Amplitude Modulation (QAM)

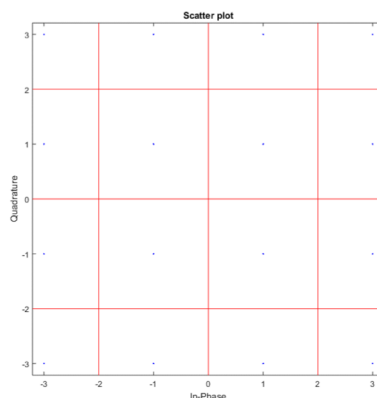
QAM

- A pulse of the carrier frequency encompasses a symbol.
- The symbol can take on a number of states, encoded as finite levels of amplitude and phase (quadrature)
- Here we need to window our sine carrier to form a pulse
- A rectangular window would produce spectral leakage, and heavy interference – use a raised cosine window
- A RCW results in no inter-symbol-interference



Constellations

- For QAM 16 – 16 discrete locations on the inphase / quadrature plane
- Red lines denote decision boundary

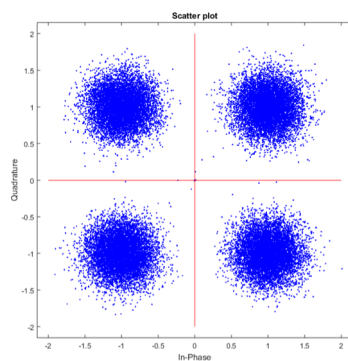


Doubling data rate – QAM4 to QAM16

- Bits per symbol of QAM4 = 2, QAM16 = 4
- Constellation diagrams
- Assuming receive power of $\frac{Eb}{No} = 10dB$, what is the probability that a message sent crosses the descision boundary?
 – $\frac{Eb}{No}$ is the energy per bit received, over the average noise energy at the receiver.



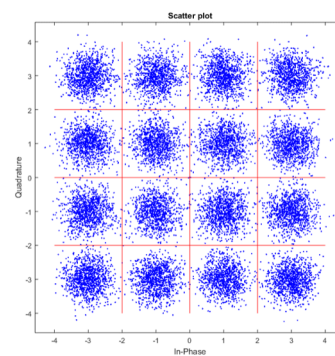
QAM4 v QAM16



$$Perr_4 = 8 \cdot 10^{-6}$$

$$BER = 4 \cdot 10^{-6}$$

$$Rate = 2 \frac{\text{Bits}}{\text{Symbol}}$$



$$Perr_{16} = 8 \cdot 10^{-3}$$

$$2 \cdot 10^{-3}$$

$$4 \frac{\text{Bits}}{\text{Symbol}}$$

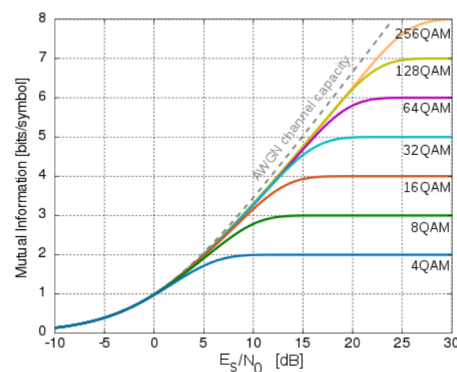


QAM4 v QAM16

- Double the data rate
- 500× more likely to flip a bit!
- Generally BER is a specification of the communication protocol
- For example Gigabit Ethernet adjusts the constellation to maintain a raw BER below 10^{-10} (one per 10 gigabits)
 - In other words, your Ethernet connection will produce ~ 7-8 one bit errors per hour of 4k Netflix streaming (~7GB/Hr)
- Source coding reduces this to 10^{-14} (one per 100 terabits)



QAM vs Theoretical maximum



- Using a smaller constellation restricts the channel capacity
- Using too high a constellation requires complex channel coding to exploit



Shannon Capacity of the AWGN channel

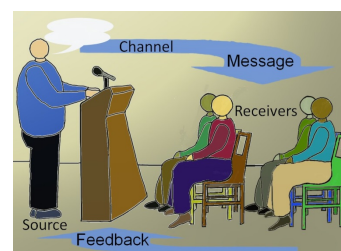
- $C = B \log_2 \left(1 + \frac{S}{N}\right)$
- B is the bandwidth S the signal power in real terms, N noise in real terms, and C the capacity in bits.
- Upper bound on error free transmission
- By intelligently selecting QAM constellation and Channel coding schema in tandem capacity can be maximised.
- Requires some coordination between transmitter and sender



Shannon and Weaver: Models of Communication

Three “problems” in Communication:

- The technical problem: how accurately can the message be transmitted?
- The semantic problem: how precisely is the meaning “conveyed”?
- The effectiveness problem: how effectively does the received meaning affect behaviour?



Source:
http://en.wikipedia.org/wiki/File:Transactional_comm_model.jpg



Ex: Morse code

- Code words are shortest for the most common letters
- This means that messages are, on average, sent more quickly.

A	• —	U	• • —
B	— • • •	V	• • — —
C	— • — •	W	• — — —
D	— • •	X	— • • —
E	•	Y	— • — —
F	• • — •	Z	— — • •
G	— — •		
H	• • • •		
I	• •		
J	• — — —		
K	— • —	1	• — — — —
L	• — • •	2	• • — — —
M	— —	3	• • • — —
N	— •	4	• • • • —
O	— — —	5	• • • • •
P	• — — •	6	— • • • •
Q	— — • —	7	— — • • •
R	• — •	8	— — — • •
S	• • •	9	— — — — •
T	—	0	— — — — —



What is the “optimal code”?

- X is a random variable
- Alice wants to tell Bob the value of X (repeatedly)
- What is the best binary code to use?
- How many bits does it take (on average) to transmit the value of X?



Optimal code lengths

- In the optimal code, the word for $X = i$ has length
- $\log_2 \frac{1}{p(X=i)} = -\log_2 p(X=i)$
- For example:

Value of X	Probability	Code word
A	$\frac{1}{2}$	0
B	$\frac{1}{4}$	10
C	$\frac{1}{4}$	11
- ABAACACBAACB coded as 010001101110001110
- If code length is not an integer, transmit many letters together



Kullback-Leibler divergence

- Measures the difference between two probability distributions
 - (Mutual information was between two random variables)
- Suppose you use the wrong code for X . How many bits do you waste?

$$\begin{aligned}
 D_{KL}(p||q) &= \sum_x p(x) \left[\log_2 \frac{1}{q(x)} - \log_2 \frac{1}{p(x)} \right] \\
 &= \sum_x p(x) \log_2 \frac{p(x)}{q(x)}
 \end{aligned}$$

Length of
codeword
Length of optimal
codeword

- $D_{KL}(p||q) \geq 0$, with equality when p and q are the same.
- $I(X; Y) = D_{KL}(p(x, y)||p(x)p(y))$



Continuous variables

- X uniformly distributed between 0 and 1.
- How many bits required to encode X to given accuracy?

Decimal places	Entropy
1	3.3219
2	6.6439
3	9.9658
4	13.2877
5	16.6096
Infinity	Infinity

- Can we make any use of information theory for continuous variables?



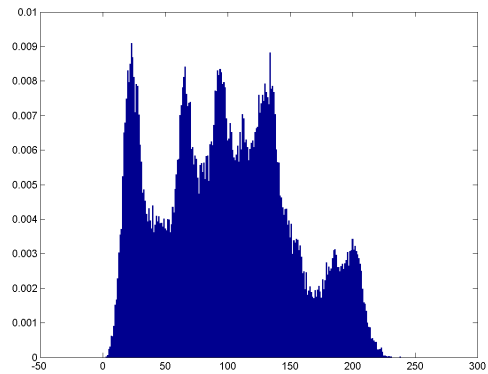
K-L divergence for continuous variables

- Even though entropy is infinite, K-L divergence is usually finite.
- Message lengths using optimal and non-optimal codes both tend to infinity as you have more accuracy. But their difference converges to a fixed number.

$$\sum_x p(x) \log_2 \frac{p(x)}{q(x)} \rightarrow \int p(x) \log_2 \frac{p(x)}{q(x)} dx$$



Calculating the Entropy of an Image



The entropy of lena is = 7.57 bits/pixel approx



Huffman Coding of Lenna

Symbol	Code Length
0	42
1	42
2	41
3	17
4	14
...	...

$$\text{Average Code Word Length} = \sum_{k=0}^{255} p_k l_k = 7.59 \text{ bits/pixel}$$

So the code length is not much greater than the entropy



But this is not very good

- Why?
 - Entropy is not the minimum average codeword length for a source with memory
 - If the other pixel values are known we can predict the unknown pixel with much greater certainty and hence the effective (ie. conditional) entropy is much less.
- Entropy Rate
 - The minimum average codeword length for any source.
 - It is defined as

$$H(\chi) = \lim_{n \rightarrow \infty} \frac{1}{N} H(X_1, X_2, \dots, X_n)$$



Coding Sources with Memory

- It is very difficult to achieve codeword lengths close to the entropy rate
 - In fact it is difficult to calculate the entropy rate itself – $P(X_1|X_2 \dots X_n)$ is described in R^n Space – for lena $n = 65536$
- We looked at LZW as a practical coding algorithm
 - Average codeword length tends to the entropy rate if the file is large enough
 - Efficiency is improved if we use Huffman to encode the output of LZW
 - LZ algorithms used in lossless compression formats (eg. .tiff, .png, .gif, .zip, .gz, .rar...)



Efficiency of Lossless Compression



- Lenna (256x256) file sizes
 - Uncompressed tiff - 64.2 kB
 - LZW tiff – 69.0 kB
 - Deflate (LZ77 + Huff) – 58 kB



- Green Screen (1920 x 1080) file sizes
 - Uncompressed – 5.93 MB
 - LZW – 4.85 MB
 - Deflate – 3.7 MB



Differential Coding

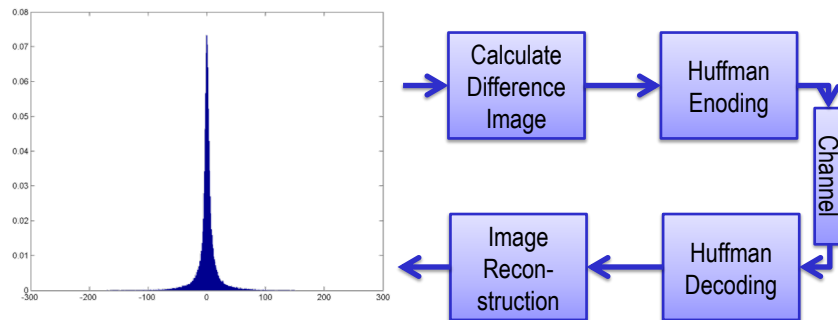
- Key idea – code the differences in intensity.



$$G(x,y) = I(x,y) - I(x-1,y)$$



Differential Coding

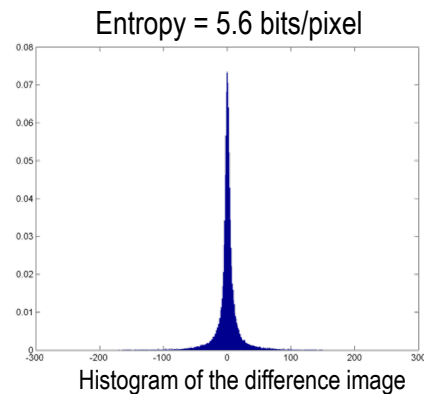
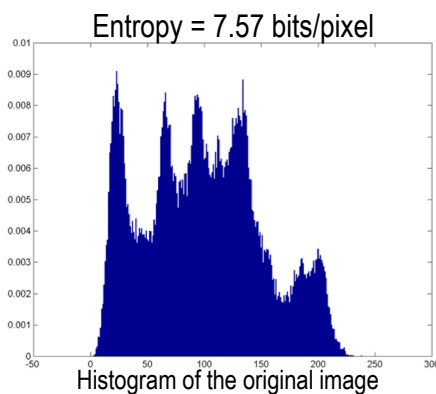


- The entropy is now 5.60 bits/pixel which is much less than 7.57 bits/pixel we had before (despite having twice as many symbols)



Entropy In General

- Entropy of a source is maximised when all signals are equiprobable and is less when a few symbols are much more probable than the others.



Lossy Compression

- But this is still not enough compression
 - Trick is to throw away data that has the least perceptual significance



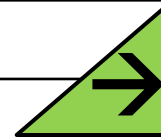
Effective bit rate = 8
bits/pixel



Effective bit rate = 1
bit/pixel (approx)



Next Time...



- **Exam Review!!**
- Review:
 - Chapter 6 of FPW
 - Chapter 13 of Lathi
- Deeper Pondering??



Final Exam **Reviews**

1. Wed, June 5, 2019

- EBESS – Loc: TBA
- 3-7pm???

2. Thursday June 6, 2019


- 12n—2p
- TBA

- [Some Review Notes](#)
(from Course Textbooks)

➔ <http://robotics.itee.uq.edu.au/~elec3004/tutes.html>

Semester One Final Examinations, 2017

ELEC3004 Signals, Systems & Control



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School of Information Technology and Electrical Engineering
EXAMINATION

Semester One Final Examinations, 2017
ELEC3004 Signals, Systems & Control
This paper is for St Lucia Campus students

Examination Duration: 180 minutes
Reading Time: 10 minutes

Exam Conditions:
This is a Central Examination
This is a Closed Book Examination - specified materials permitted
During reading time - write only on the rough paper provided
This examination paper will be released to the Library

Materials Permitted in The Exam Venue:
(No electronic aids are permitted e.g. laptops, phones)
Calculators - Any calculator permitted - unrestricted
One A4 sheet of handwritten or typed notes double sided is permitted

Materials To Be Supplied To Students:
1 x 14 Page Answer Booklet
1 x 1cm x 1cm Graph Paper

Instructions To Students:
Additional exam materials (eg. answer booklets, rough paper) will be provided upon request.
Please answer all questions. Thank you! :)

Q	Mark
1	
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Total: _____

Page 1 of 14



ELEC 3004: Systems

Fun Fact: With this, 42% of the exam is already "public" 😊

29 May 2019 - 67