

→ SPNS- 4/21/2015 - ELEC 3004 -

WINDOWING

$$y[n] = \underbrace{h[n]}_{\text{LPF | HPF | ETC.}} \cdot \underbrace{x[n]}_{\text{SIGNAL}}$$

$w[n]$: window function

↳ finite duration FBA

$$\hookrightarrow w[n] = \begin{cases} 1 & \text{for } a \leq n \leq b, \\ 0 & n < a \text{ or } n > b \end{cases}$$

$$\Rightarrow \begin{aligned} X_w[n] &= x[n] \cdot w[n] \\ h_w[n] &= h[n] \cdot w[n] \end{aligned}$$

where $w[n] = 0$ for $n < 0$, $n \geq N$

∴ we define the window for a sequence of length N

TWO CASES

1) SPECTRAL ANALYSIS

2) FIR FILTER DESIGN.

1) SPECTRAL ANALYSIS $\Leftrightarrow X$

↳ GPAR: process a finite length of data

$$\text{DTFT} \quad X_w(e^{j\omega}) = \frac{1}{2\pi} X(e^{j\omega}) * W(e^{j\omega})$$

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III • peak side level $\Rightarrow$ DYNAMIC RANGE

• ~~the~~ Mainlobe $\Rightarrow$ Resolution of the spectral estimator

IV FIR FILTERS $\Leftrightarrow$ HW

$$hw[n] = h[n] \cdot w[n]$$